



上海交通大学
SHANGHAI JIAO TONG UNIVERSITY



Lecture 20

Transistor Amplifiers (II)



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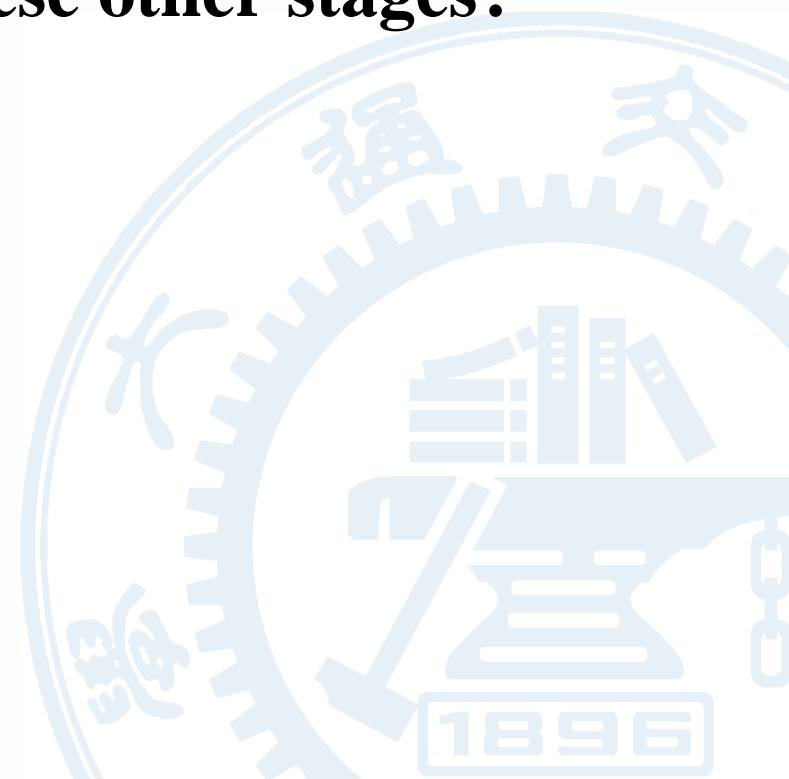
- **Common-drain amplifier**
- **Common-gate amplifier**





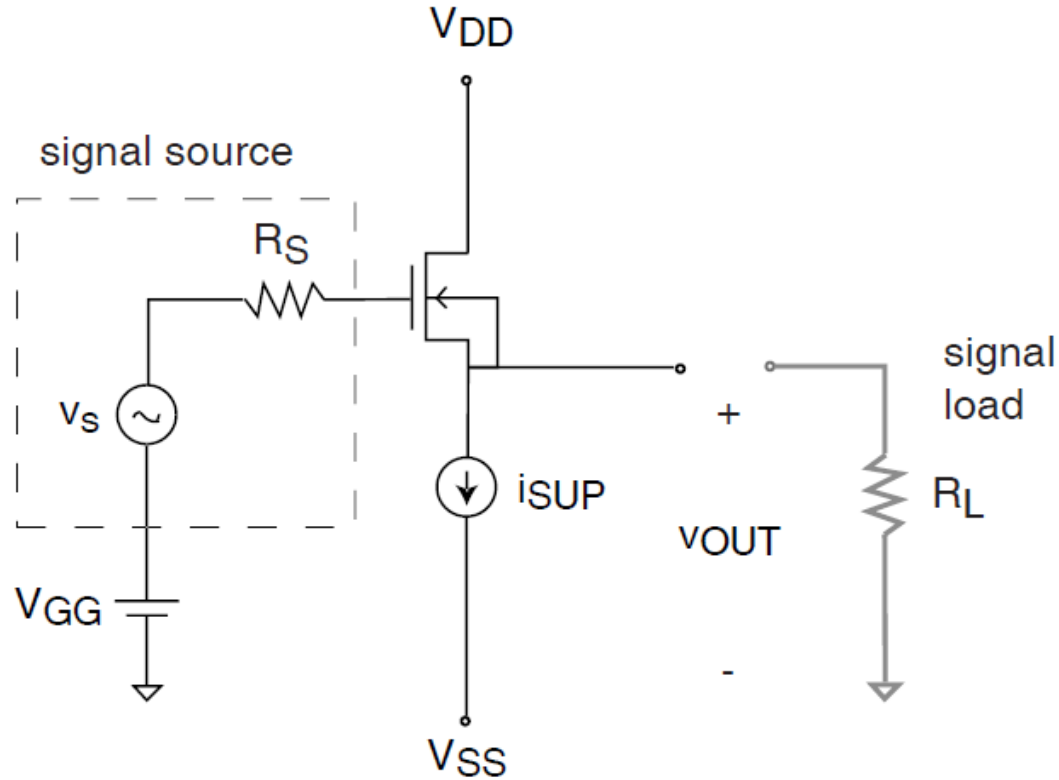
Key questions

- **What other amplifier stages can one build with a single MOSFET and a current source?**
- **What is the uniqueness of these other stages?**





2. Common-drain amplifier





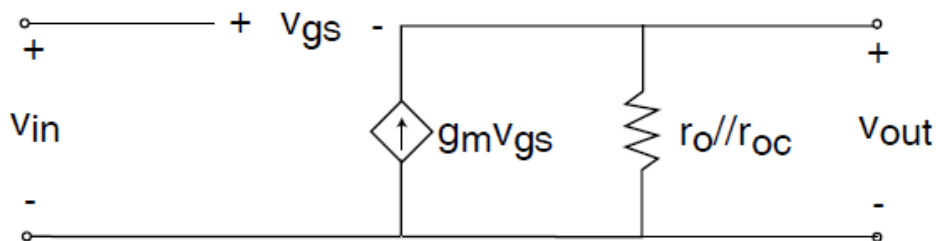
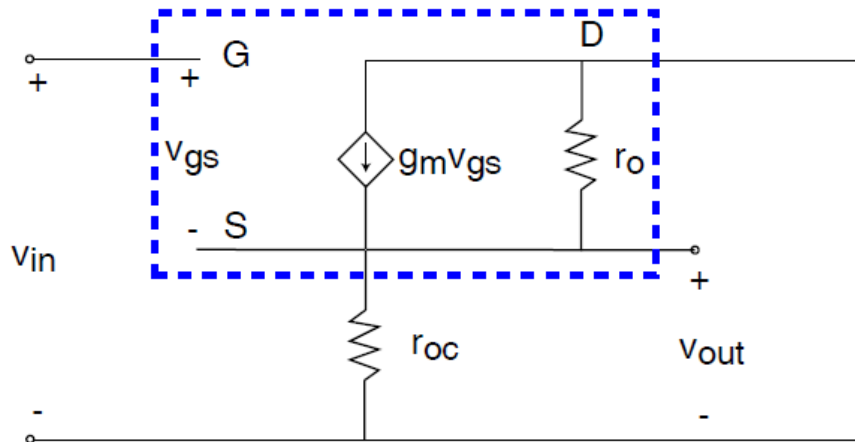
How does it work?

- V_{GG} , I_{SUP} , and W/L selected to bias MOSFET in saturation, obtain desired output bias point, and desired output swing.
- $v_{GG} \uparrow \Rightarrow i_D$ can't change $\Rightarrow v_{OUT} \uparrow$ (source follower)
- to first order, no voltage gain: $v_{out} \cong v_s$
- but R_{out} small: effective voltage buffer stage (good for making voltage amp in combination with common-source stage).



□ Small-signal analysis

Unloaded small-signal equivalent circuit model:



$$v_{in} = v_{gs} + v_{out}$$

$$v_{out} = g_m v_{gs} (r_o // r_{oc})$$

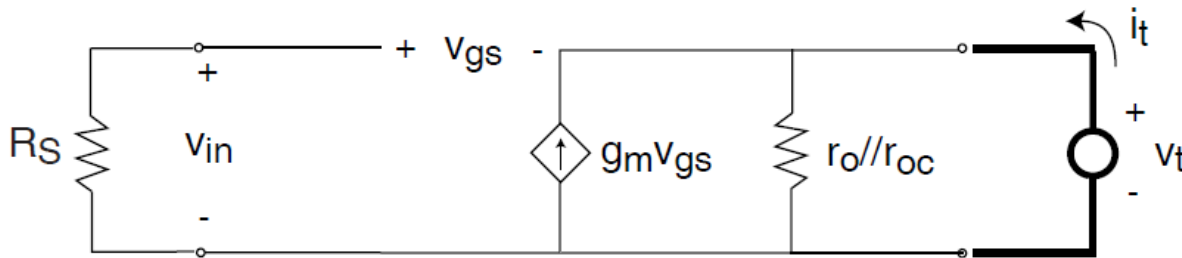
Then:

$$A_{vo} = \frac{g_m}{g_m + \frac{1}{r_o // r_{oc}}} \approx 1$$



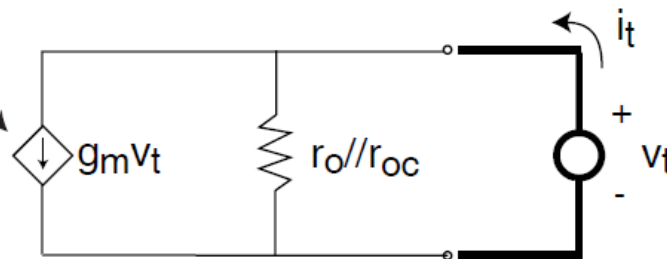
Input impedance: $R_{in} = \infty$

Output impedance:



$v_{gs} = -v_t$

effectively:
resistance of
value $1/g_m$



$$R_{out} = \frac{1}{g_m + \frac{1}{r_o // r_{oc}}} \approx \frac{1}{g_m}$$

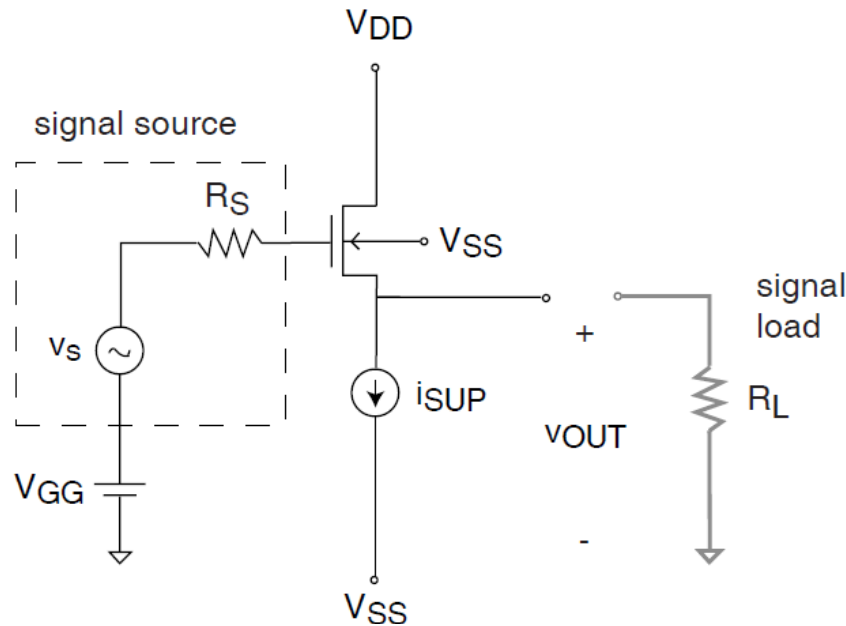
Small!

Loaded voltage gain: $A_v = A_{vo} \frac{R_L}{R_L + R_{out}} \approx \frac{R_L}{R_L + \frac{1}{g_m}} \approx 1$



Effect of back bias:

If MOSFET not fabricated on isolated p-well, then body is tied up to wafer substrate (connected to V_{SS}):



Two consequences:

Bias affected: V_T depends on $V_{BS} = V_{SS} - V_{OUT} \neq 0$

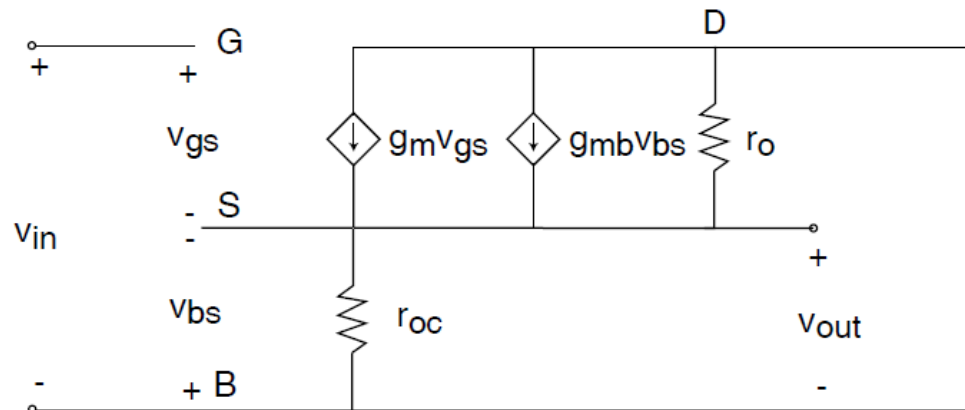
Small signal figures of merit affected: signal shows up between B and S

($v_{BS} = -v_{out}$).

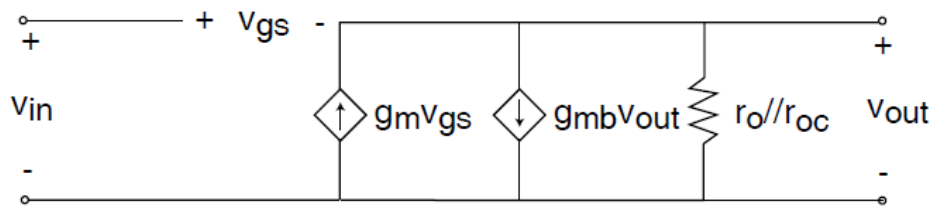




Small signal equivalent circuit model:



↓ $V_{bs} = -V_{out}$



$$A_{vo} = \frac{g_m}{g_m + g_{mb} + \frac{1}{r_o // r_{oc}}} \approx \frac{g_m}{g_m + g_{mb}} < 1 \quad R_{out} = \frac{1}{g_m + g_{mb} + \frac{1}{r_o // r_{oc}}} \approx \frac{1}{g_m + g_{mb}}$$



□ Relationship between circuit figures of merit and device parameters:

$$g_m = \sqrt{2 \frac{W}{L} \mu_n C_{ox} I_D} \quad g_{mb} = \frac{\gamma}{2\sqrt{-2\phi_p - V_{BS}}} g_m$$

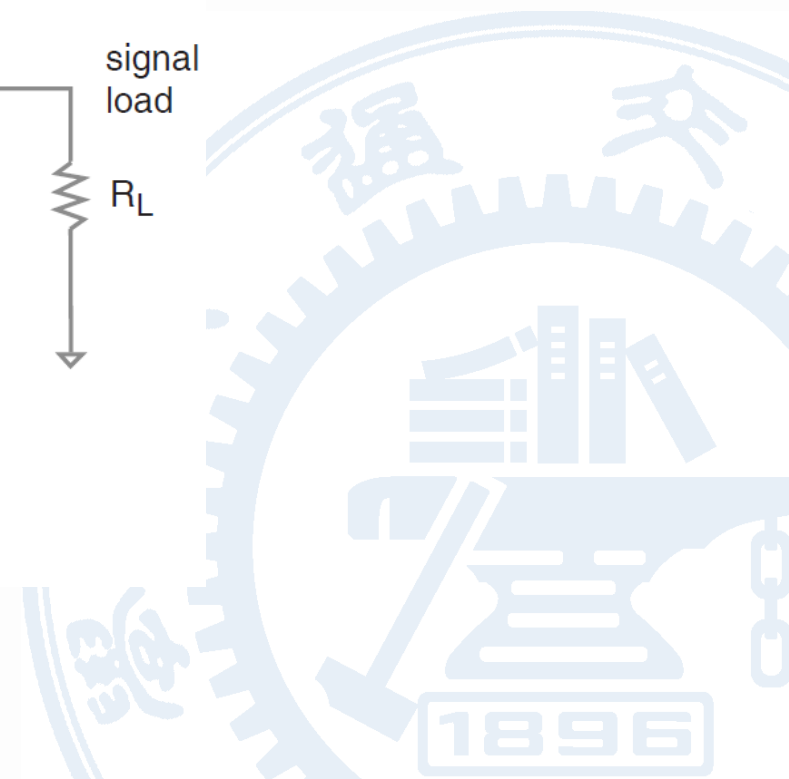
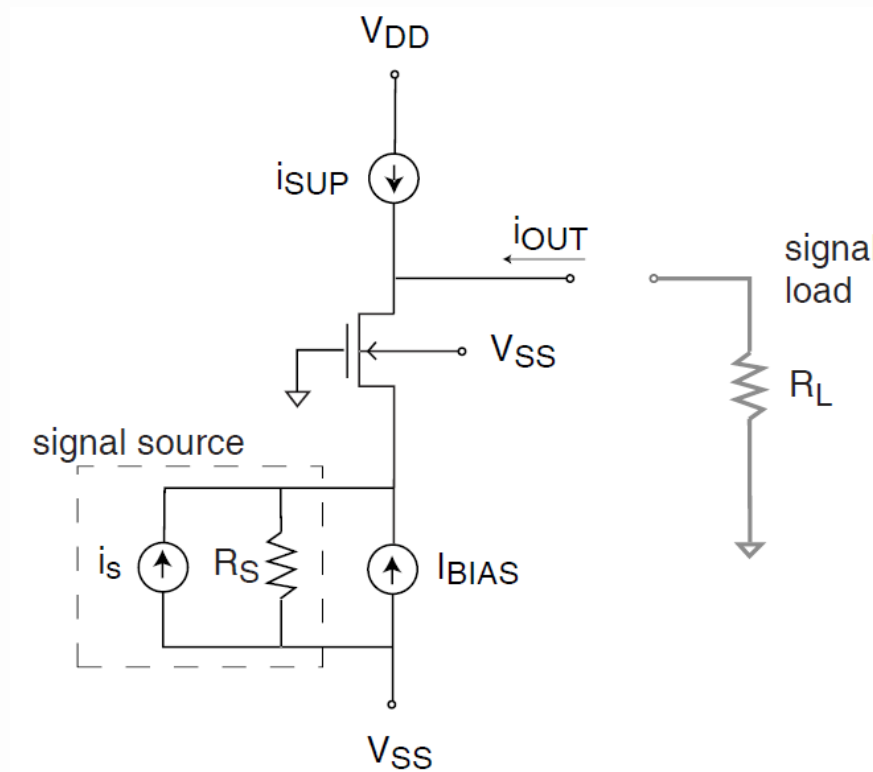
Device * Parameters	Circuit Parameters		
	$ A_{vo} $	R_{in}	R_{out}
	$\frac{g_m}{g_m + g_{mb}}$	∞	$\frac{1}{g_m + g_{mb}}$
$I_{SUP} \uparrow$	-	-	\downarrow
$W \uparrow$	-	-	\downarrow
$\mu_n C_{ox} \uparrow$	-	-	\downarrow
$L \uparrow$	-	-	\uparrow

CD amp useful as a voltage buffer to drive small loads (in a multistage amp, other stages will be used to provide voltage gain).



3. Common gate amplifier

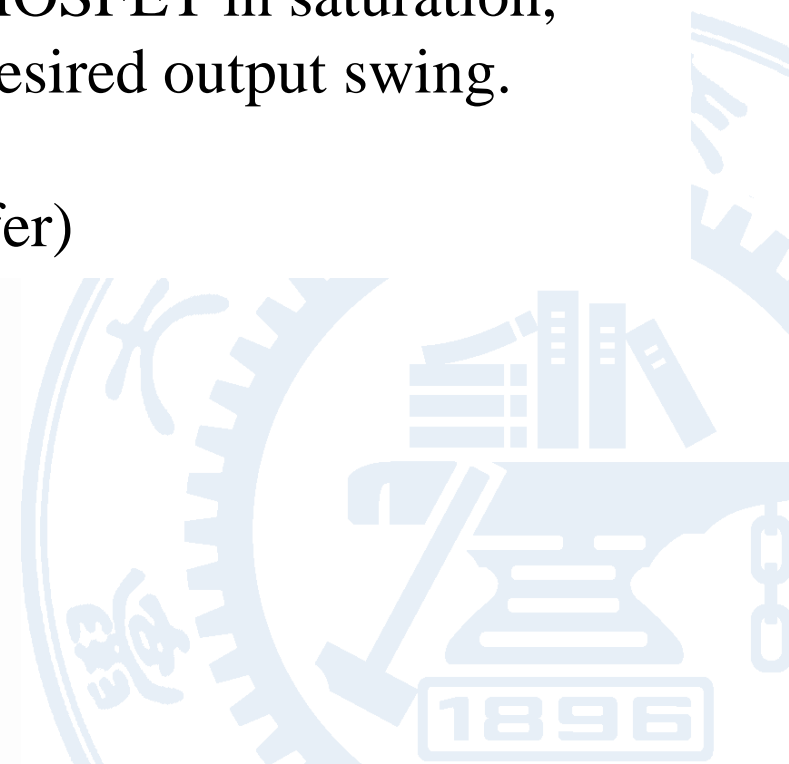
Need to handle current mode signal sources:





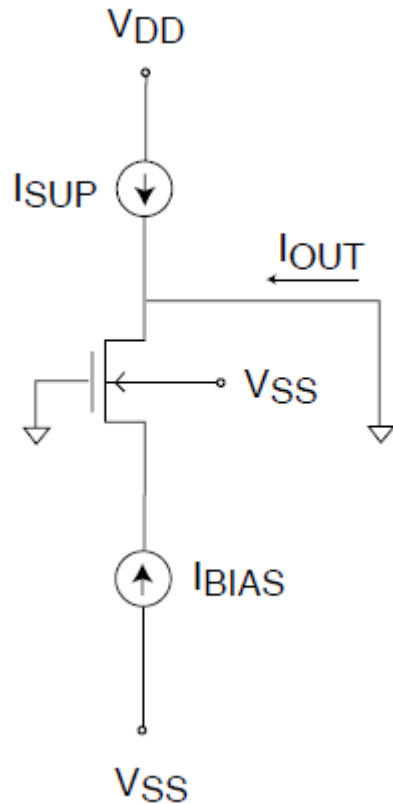
How does it work?

- Since source is signal input terminal, body cannot be tied up to source (C_{sb} is significant)
- i_{SUP} , I_{BIAS} , and W/L selected to bias MOSFET in saturation, obtain desired output bias point, and desired output swing.
- no current gain: $i_s = i_{out}$ (current buffer)





□ Bias: select I_{SUP} , I_{BIAS} , and W/L to get proper quiescent I_{OUT} and keep MOSFET in saturation



$$I_{SUP} + I_{OUT} + I_{BIAS} = 0$$

Select bias so that $I_{OUT}=0 \Rightarrow V_{OUT}=0$.

Assume MOSFET in saturation
(no channel modulation):

$$I_D = \frac{W}{2L} \mu_n C_{ox} (V_{GS} - V_T)^2 = I_{SUP} = -I_{BIAS}$$

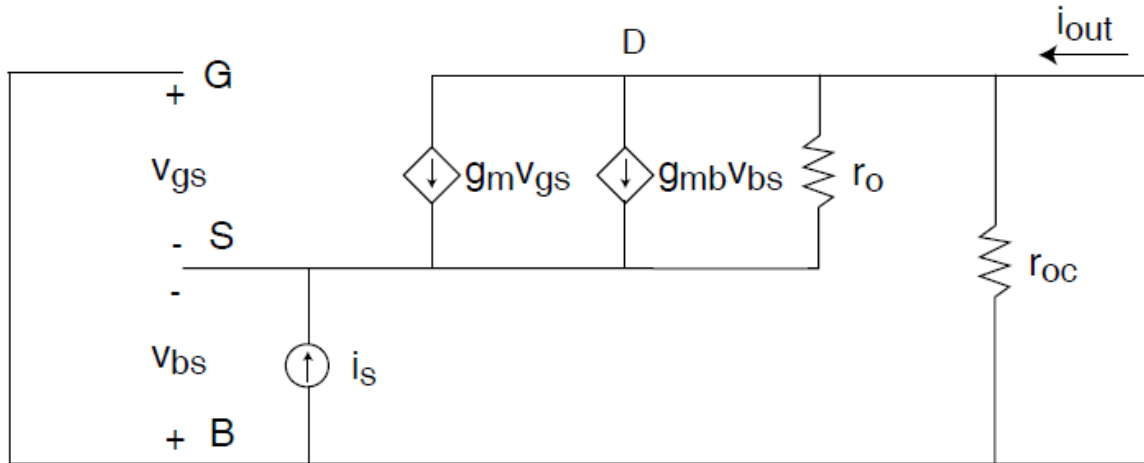
but V_T depends on V_{BS} :

$$V_T = V_{To} + \gamma_n (\sqrt{-2\phi_p - V_{BS}} - \sqrt{-2\phi_p})$$

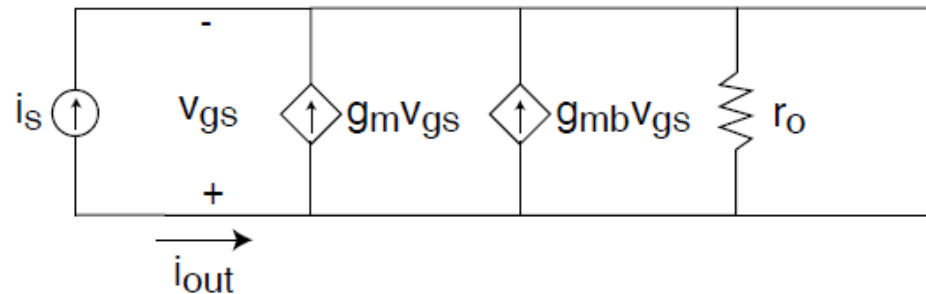
Must solve these two equations iteratively to get V_S .

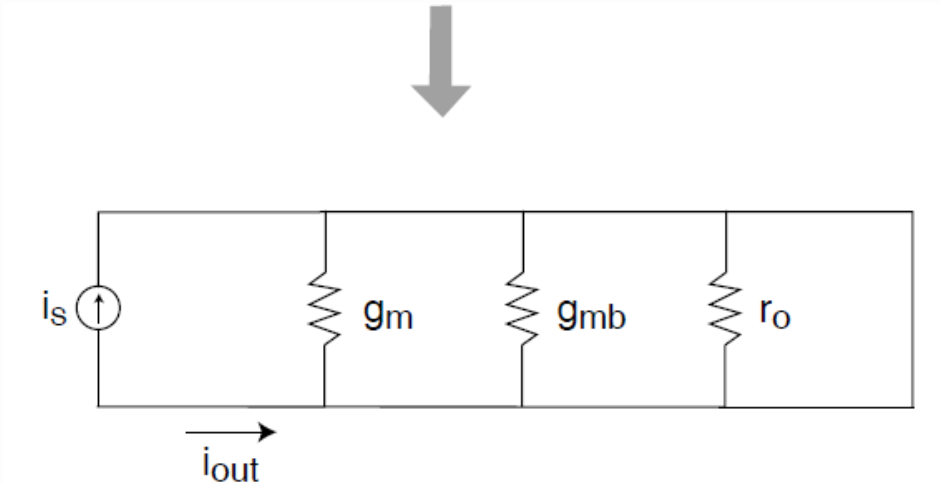


□ Small signal circuit (unloaded)



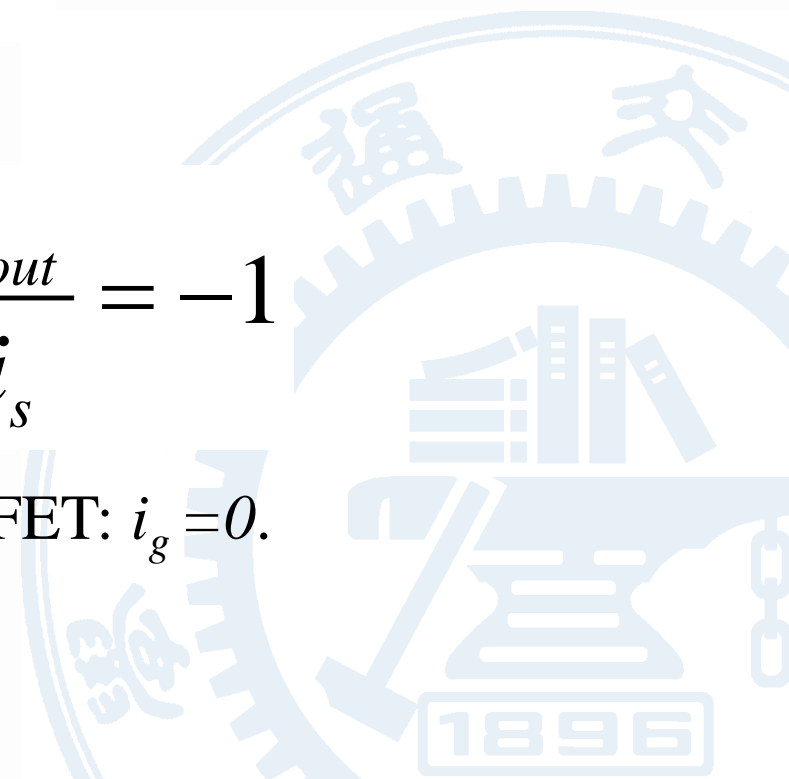
$$V_{bs} = V_{gs}$$





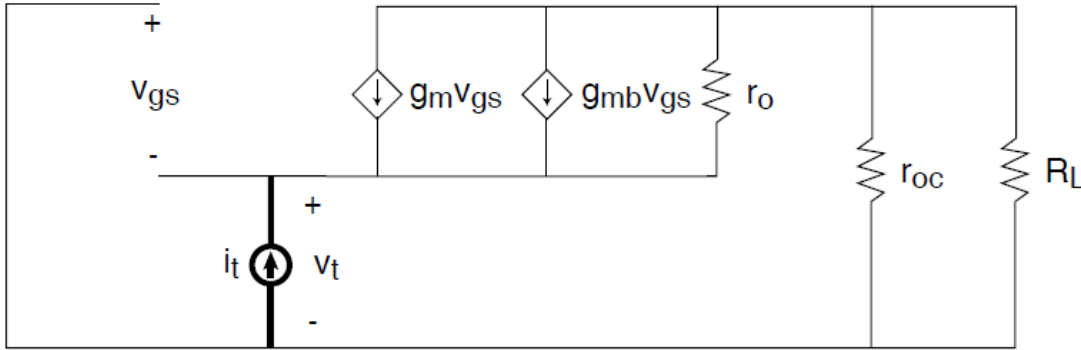
$$i_s = -i_{out} \Rightarrow A_{io} = -\frac{i_{out}}{i_s} = -1$$

Not surprising, since in a MOSFET: $i_g = 0$.

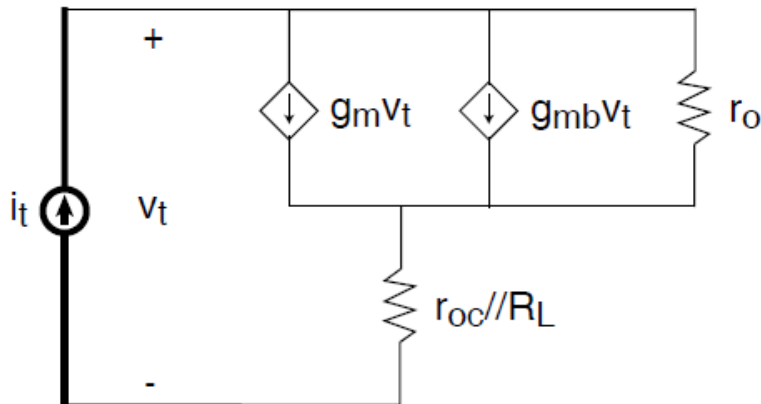




Input resistance:



↓ $v_{gs} = -v_t$



Do KCL on input node:

$$i_t - g_m v_t - g_{mb} v_t - \frac{v_t - (r_{oc} // R_L) i_t}{r_o} = 0$$

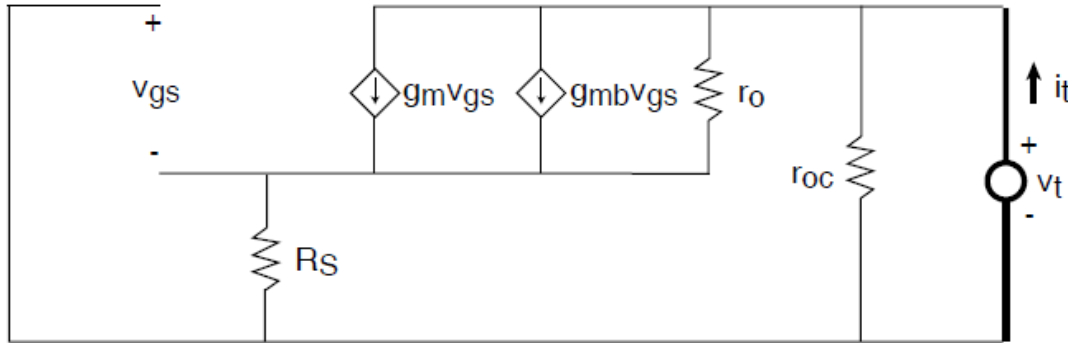
Then:

$$R_{in} = \frac{1 + \frac{r_{oc} // R_L}{r_o}}{g_m + g_{mb} + \frac{1}{r_o}} \approx \frac{1}{g_m + g_{mb}}$$

Very small.



Output resistance:



Do KCL on output node:

$$i_t' - g_m v_{gs} - g_{mb} v_{gs} - \frac{v_t' + v_{gs}}{r_o} = 0$$

Notice also:

$$v_{gs} = -i_t' R_S$$

Then:

$$R_{out} = r_{OC} // \left\{ r_o \left[1 + R_S \left(g_m + g_{mb} + \frac{1}{r_o} \right) \right] \right\} \approx r_{OC} // [r_o (1 + g_m R_S)]$$

Very large, because of the feedback effect of R_S .



Summary of MOSFET amplifier stages:

stage	A_{vo}, G_{mo}, A_{io}	R_{in}	R_{out}	key function
common source	$G_{mo} = g_m$	∞	$r_o // r_{oc}$	transconductance amp.
common drain	$A_{vo} \simeq \frac{g_m}{g_m + g_{mb}}$	∞	$\frac{1}{g_m + g_{mb}}$	voltage buffer
common gate	$A_{io} \simeq -1$	$\frac{1}{g_m + g_{mb}}$	$r_{oc} // [r_o(1 + g_m R_S)]$	current buffer

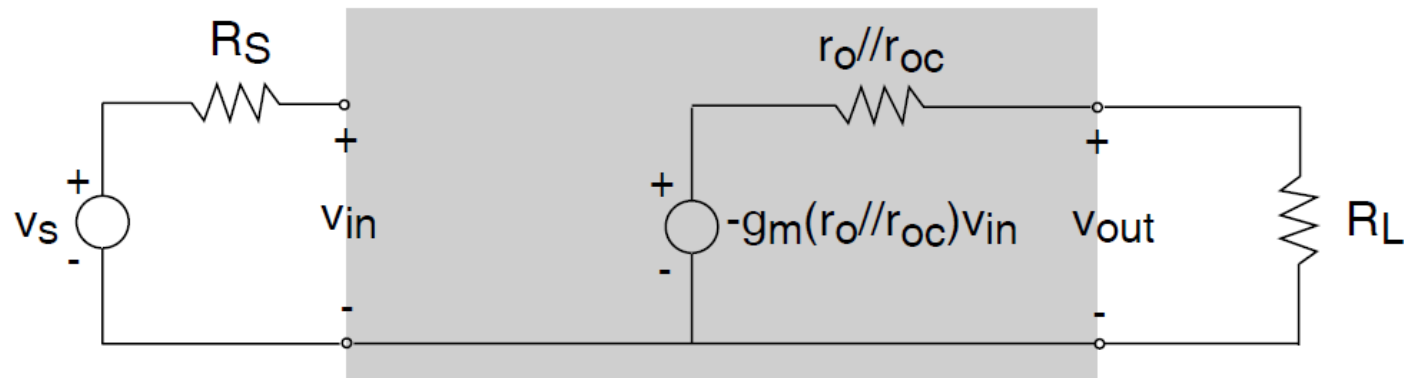
In order to design amplifiers with suitable performance, need to combine these stages
 \Rightarrow multistage amplifiers



□ CMOS multistage voltage amplifier

Goals:

- high voltage gain
- high R_{in}
- low R_{out}
- Good starting point: CS stage



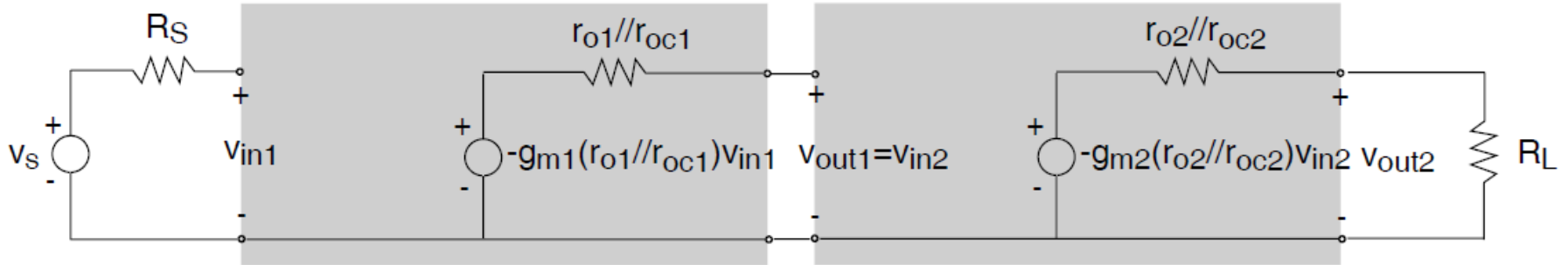
$$R_{in} = \infty$$

$$A_{vo} = -g_m (r_o // r_{oc}), \text{ probably insufficient}$$

$$R_{out} = r_o // r_{oc}, \text{ too high}$$



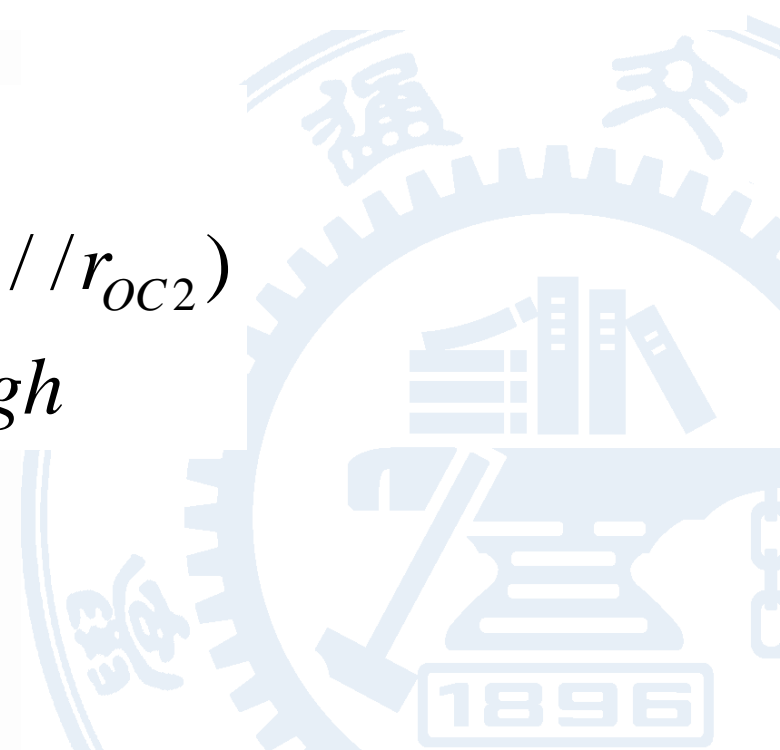
□ Add second CS stage to get more gain:



$$R_{in} = \infty$$

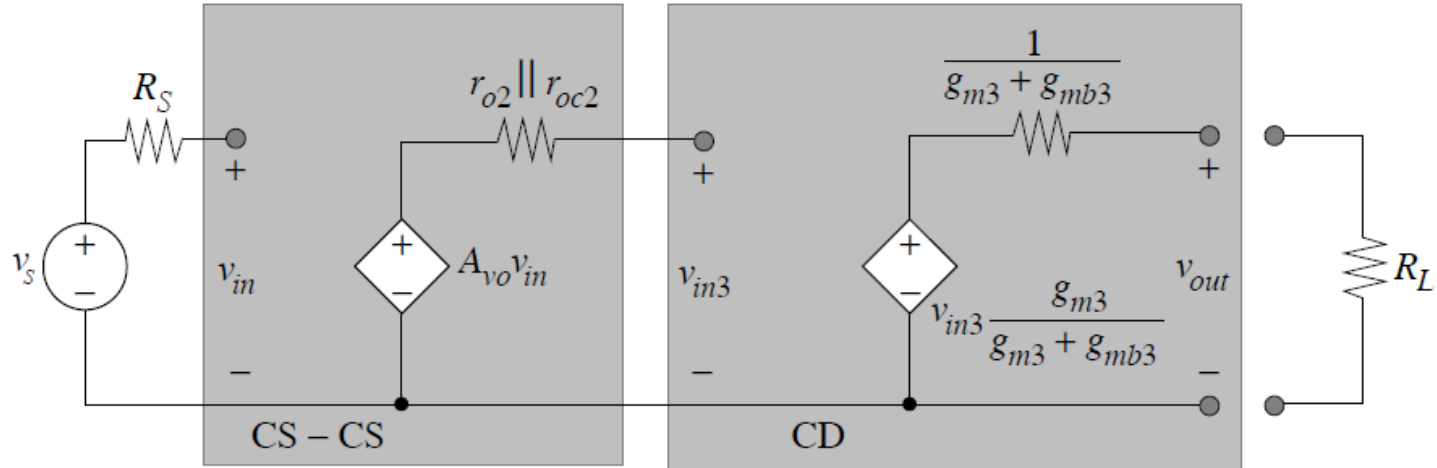
$$A_{vo} = g_{m1}(r_{o1} // r_{oc1})g_{m2}(r_{o2} // r_{oc2})$$

But $R_{out} = r_{o2} // r_{oc2}$, still high





□ Add CD stage at output:



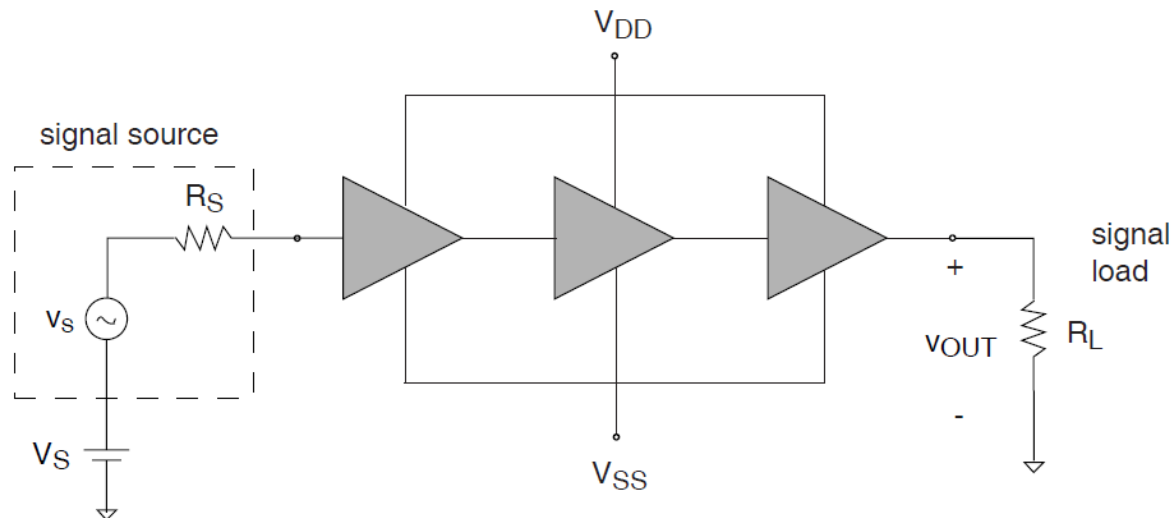
$$R_{in} = \infty$$

$$A_{vo} = g_{m1}(r_{o1} // r_{oc1})g_{m2}(r_{o2} // r_{oc2}) \frac{g_{m3}}{g_{m3} + g_{mb3}}, \text{ still high}$$

$$R_{out} = \frac{1}{g_{m3} + g_{mb3}}, \text{ now small}$$



- ◆ Amplifier requirements are often demanding:
 - must adapt to specific kinds of signal source and load,
 - must deliver sufficient gain
- ◆ Single-transistor amplifier stages are very limited in what they can accomplish
⇒ multistage amplifier.





Key conclusions

Different MOSFET stages designed to accomplish different goals:

- Common-source stage:

- large voltage gain and transconductance, high input resistance, large output resistance

- excellent transconductance amplifier, reasonable voltage amplifier

- Common-drain stage:

- no voltage gain, but high input resistance and low output resistance

- good voltage buffer

- Common-gate stage:

- no current gain, but low input resistance and high output resistance

- good current buffer